

Model Question Paper
Differential Calculus Part I - Part IV
12th Standard

Maths

Reg.No. :

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I. Answer all questions.

II. Use blue pen only.

Time : 01:00:00 Hrs

Total Marks : 85

3 x 1 = 3

Section-A

- 1) The parametric equations of the curve $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$ are
(a) $x = a \sin^3 \theta; y = a \cos^3 \theta$ (b) $x = a \cos^3 \theta; y = a \sin^3 \theta$ (c) $x = a^3 \sin \theta; y = a^3 \cos \theta$ (d) $x = a^3 \cos \theta; y = a^3 \sin \theta$
- 2) Let "h" be the height of the tank. Then the rate of change of pressure "p" of the tank with respect to height is
(a) $\frac{dh}{dt}$ (b) $\frac{dp}{dt}$ (c) $\frac{dh}{dp}$ (d) $\frac{dp}{dh}$
- 3) If the temperature $\theta^\circ C$ of the certain metal rod of "l" meters is given by $l = 1 + 0.00005 \theta + 0.0000004 \theta^2$ then the rate of change of l in m / C° when the temperature is $100^\circ C$ is
(a) $0.00013 \text{ m}/C^\circ$ (b) $0.00023 \text{ m}/C^\circ$ (c) $0.00026 \text{ m}/C^\circ$ (d) $0.00033 \text{ m}/C^\circ$

Section-B

9 x 6 = 54

- 4) A Particle of unit mass moves so that displacement after t secs is given by $x = 3\cos(2t - 4)$. Find the acceleration and kinetic energy at the end of 2 secs.
[K. E. = $\frac{1}{2}mv^2$, m is mass]
- 5) Newton's law of cooling is given by $\theta = \theta_0 e^{-kt}$, where the excess of temperature at zero time is $\theta_0^\circ C$ and time t seconds is $\theta^\circ C$. Determine the rate of change of temperature after 40s, given that $\theta_0 = 16^\circ C$ and at time $k = -0.03$. ($e^{1.2} = 3.3201$)
- 6) Two sides of a triangle are 4m and 5m in length and the angle between them is increasing at a rate of 0.06 rad/sec . Find the rate at which the area of the triangle is increasing when the angle between the sides of fixed length is $\pi/3$.
- 7) Show that $x^2 - y^2 = a^2$ and $xy = c^2$ cut orthogonally.
- 8) Find the equation of the tangent and normal to the curves $y = x^2 - 4x - 5$ at $x = -2$
- 9) Find the absolute maximum and absolute minimum values of f on the given interval: $f(x) = x - 2\cos x$, $[-\pi, \pi]$
- 10) Prove the following inequalities: $\sin x > x - \frac{x^3}{6}$, $x > 0$
- 11) Prove the following inequalities: $\tan^{-1} x < x$ for all $x > 0$
- 12) Prove the following inequalities: $\log(1+x) < x$ for all $x > 0$

Section-C

4 x 10 = 40

- 13) A missile fired from ground level rises x metres vertically upwards in t seconds and $x = 100t - \frac{25}{2}t^2$. Find (i) the initial velocity of the missile, (ii) the time when the height of the missile is a maximum (iii) the maximum height reached and (iv) the velocity with which the missile strikes the ground.
- 14) The distance x metres traveled by a vehicle in time t seconds after the brakes are applied is given by: $x = 20t - 5/3t^2$. Determine (i) the speed of the vehicle (in km/hr) at the instant the brakes are applied and (ii) the distance the car traveled before it stops.
- 15) a) The altitude of a triangle is increasing at a rate of 1 cm/min while the area of the triangle is increasing at a rate of $2 \text{ cm}^2/\text{min}$. At what rate is the base of the triangle changing when the altitude is 10 cm and the area is 100 cm^2 .

(OR)

- b) At noon, ship A is 100 km west of ship B. Ship A is sailing east at 35 km/hr and ship B is sailing north at 25 km/hr . How fast is the distance between the ships changing at 4.00 p.m.
