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HIGHER SECONDARY FIRST YEAR

MATHEMATICS

MODEL QUESTION PAPER

Time Allowed: 2.30 Hours]

Instructions:

(1) 3

[Maximum Marks:90

- Check the question paper for fairness of printing. If there (a) is any lack of fairness, inform the Hall Supervisor immediately.
- Use **Blue** or **Black** ink to write and underline and pencil to (b)draw diagrams.

<u>SECTION – I</u>

 $20 \times 1 = 20$ Note: (i) All questions are compulsory. Choose the correct or most suitable answer from the given four (ii) alternatives. Write the option code and the corresponding answer. 1. If two sets A and B have 17 elements in common, then the number of elements common to the set $A \times B$ and $B \times A$ is $(1) 2^{17}$ $(2) 17^2$ (4) insufficient data (3)342. If \mathbb{R} is the set of all real numbers and if $f: \mathbb{R} - \{3\} \to \mathbb{R}$ is defined by $f(x) = \frac{3+x}{3-x}$ for $x \in \mathbb{R} - \{3\}$, then the range of *f* is (3) $\mathbb{R} - \{-1\}$ (4) $\mathbb{R} - \{-3\}$ (1) \mathbb{R} (2) $\mathbb{R} - \{1\}$ 3. If the sum and product of the roots of the equation $2x^2 + (a-3)x + 3a - 5 = 0$ are equal, then the value of *a* is (1)1(2) 2(3)0(4) 44. Which one of the following is not true? (1) $|\sin x| \le 1$ (2) $|\sec x| < 1$ (3) $|\cos x| \le 1$ (4) $\operatorname{cosec} x \ge 1$ or $\operatorname{cosec} x \le -1$ 5. $\cos 1^{\circ} + \cos 2^{\circ} + \cos 3^{\circ} + \dots + \cos 179^{\circ}$ is (3) - 1(1)0(2)1(4) 896. If 10 lines are drawn in a plane such that no two of them are parallel and no three are concurrent, then the total number of points of intersection are $(4) 2^{10}$ (1) 45 (2) 40(3) 10! 7. The remainder when 2^{2020} is divided by 15 is (1) 4(2) 8(3)1(4) 28. The harmonic mean of two positive numbers whose arithmetic mean and geometric mean are 16, 8 respectively is (1)10(2)6(3)5(4)49. In the equation of a straight line ax + by + c = 0, if a,b,c are in arithmetic progression then the point on the straight line is (1) (1,2)(2) (1,-2)(3) (2,-1)(4) (2,1)10. If two straight lines x + (2k-7)y + 3 = 0 and 3kx + 9y - 5 = 0 are perpendicular to each other then the value of k is $(3)\frac{2}{2}$ $(2)\frac{1}{2}$ $(4)\frac{3}{2}$

QB365 https://www.qb365.in/materials/ 11. If $|\vec{a}| = 13$, $|\vec{b}| = 5$ and $\vec{a} \cdot \vec{b} = 60^{\circ}$ then $|\vec{a} \times \vec{b}|$ is (1) 15(2)35(4) 25(3)4512. A vector \overrightarrow{OP} makes 60° and 45° with the positive direction of the x and y axes respectively. Then the angle between \overrightarrow{OP} and the z-axis is (2) 60° (4) 30° $(1) 45^{\circ}$ (3) 90° 13. A vector perpendicular to both $\hat{i} + \hat{j} + \hat{k}$ and $2\hat{i} + \hat{j} + 3\hat{k}$ is, (1) $2\hat{i} + \hat{j} - \hat{k}$ (2) $2\hat{i} - \hat{j} - \hat{k}$ (3) $3\hat{i} + \hat{j} + 2\hat{k}$ (4) $3\hat{i} + \hat{j} - 2\hat{k}$ 14. $\lim_{x \to 0} \frac{\sin |x|}{r}$ is (3)0 (4) does not exist (1)1(2) - 115. If $f: \mathbb{R} \to \mathbb{R}$ is defined by $f(x) = \lfloor x - 3 \rfloor + \lfloor x - 4 \rfloor$, $x \in \mathbb{R}$, then $\lim_{x \to 3^-} f(x)$ is equal to (3) 0 (2) - 1(4)116. If $f(x) = \begin{cases} x^3, & x < 0 \\ 3a + x^2, & x \ge 0 \end{cases}$ is continuous at x = 0, then a is (2) - 1(1) - 2(3) 0 (4) 117. The derivative of f(x) = x|x| at x = -3 is (1) 6(2) - 6(3) does not exist (4) 018. $\int \frac{dx}{x(x+1)}$ is (1) $\log \left| \frac{x+1}{r} \right| + c$ (2) $\log \left| \frac{x}{r+1} \right| + c$ (3) $\log \left| \frac{x-1}{r} \right| + c$ (4) $\log \left| \frac{x}{r-1} \right| + c$ 19. $\int 2^{3x+5} dx$ is $(1)\frac{3(2^{3x+5})}{\log 2} + c$ $(2)\frac{2^{3x+5}}{2\log(3x+5)} + c$ $(3)\frac{2^{3x+5}}{2\log 3} + c$ $(4)\frac{2^{3x+5}}{3\log 2} + c$ 20. If X and Y be two events such that $P(X/Y) = \frac{1}{2}$, $P(Y/X) = \frac{1}{3}$ and $P(X \cap Y) = \frac{1}{6}$, then $P(X \cup Y)$ is $(2)\frac{2}{5}$ $(1)\frac{1}{2}$ $(3)\frac{1}{6}$ $(4)\frac{2}{2}$ **SECTION – II** $7 \times 2 = 14$ Note: (i) Answer any **SEVEN** questions. (ii) Question number 30 is compulsory. 21. From the graph $y = \cos x$, draw $|y| = \cos x$. 22. If $\frac{\log(x)}{v-z} = \frac{\log(y)}{z-x} = \frac{\log(z)}{x-y}$, then prove that xyz = 1.

- 23. Show that $\tan(45^{\circ} A) = \frac{1 \tan A}{1 + \tan A}$
- 24. How many ways are there to arrange the letters of the word "GARDEN" with vowels in the alphabetical order.
- 25. Find the sum $1 + \frac{4}{5} + \frac{7}{25} + \frac{10}{125} + \cdots$
- 26. Show that the points whose position vectors are $2\hat{i} + 3\hat{j} 5\hat{k}$, $3\hat{i} + \hat{j} 2\hat{k}$ and $6\hat{i} 5\hat{j} + 7\hat{k}$ are collinear.

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- 27. Examine the continuity of the function $\frac{x^2 16}{x + 4}$
- 28. Find the derivative of $y = \log_{10} x$ with respect to x.

29. Evaluate:
$$\int \frac{\sin x}{1 + \cos x} dx$$

30. If $A = \begin{bmatrix} 4 & 2 \\ -1 & x \end{bmatrix}$ and $(A - 2I)(A - 3I) = O$, find the value of x.

SECTION – III

Note:

(i)

Answer any **SEVEN** questions. $7 \times 3 = 21$

(ii) Question number 40 is compulsory.

- 31. Check the relation $R = \{(1,1), (2,2), (3,3), \dots, (n,n)\}$ defined on the set $S = \{1,2,3,\dots,n\}$ for the three basic relations.
- 32. Prove that $\frac{\cot(180^\circ + \theta)\sin(90^\circ \theta)\cos(-\theta)}{\sin(270^\circ + \theta)\tan(-\theta)\csc(360^\circ + \theta)} = \cos^2\theta\cot\theta.$
- 33. In an examination a student has to answer 5 questions out of 9 questions, in which 2 are compulsory. In how many ways a student can answer the questions?

34. Find the coefficient of
$$x^{15}$$
 in $\left(x^2 + \frac{1}{x^3}\right)^{10}$

35. Find the equations of the straight lines, making the *y*-intercept of 7 and angle between the line and the *y*-axis is 30° .

36. Prove that
$$\begin{vmatrix} 1 & 1 & 1 \\ x & y & z \\ x^2 & y^2 & z^2 \end{vmatrix} = (x-y)(y-z)(z-x).$$

- 37. If \vec{a} , \vec{b} and \vec{c} are vectors with magnitudes 3,4 and 5 respectively and $\vec{a} + \vec{b} + \vec{c} = \vec{0}$, then find the value of $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$.
- 38. Evaluate : $\int x \log x \, dx$.
- 39. If *A* and *B* are mutually exclusive events $P(A) = \frac{3}{8}$ and $P(B) = \frac{1}{8}$, then find

(i)
$$P(\overline{A})$$
 (ii) $P(A \cup B)$ (iii) $P(\overline{A} \cap B)$

40. Evaluate : $\lim_{x\to 0} \frac{\sqrt{x+2}-\sqrt{2}}{x}$.

SECTION – IV

 $7 \times 5 = 35$

Note: Answer all the questions.

41. (a) If $f,g:\mathbb{R}\to\mathbb{R}$ are defined by f(x)=|x|+x and g(x)=|x|-x, find $g\circ f$ and $f\circ g$.

(OR)

(b) Solve the linear inequalities and exhibit the solution set graphically:

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 $x + y \ge 3$, $2x - y \le 5$, $-x + 2y \le 3$.

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- 42. (a) If $A + B + C = \pi$, prove that $\cos A + \cos B + \cos C = 1 + 4\sin\left(\frac{A}{2}\right)\sin\left(\frac{B}{2}\right)\sin\left(\frac{C}{2}\right)$
 - (OR)
 - (b) In a $\triangle ABC$, prove that $a\cos A + b\cos B + c\cos C = 2a\sin B\sin C$.
- 43. (a) Prove by the principle of mathematical induction, the sum of the first *n* non-zero even numbers is $n^2 + n$.

(OR)

(b) The number of bacteria in a certain culture doubles every hour. If there were 30 bacteria present in the culture originally, how many bacteria will be present at the end of 2^{nd} hour, 4^{th} hour and the n^{th} hour?

44. (a) Show that
$$\begin{vmatrix} \log x & \log y & \log z \\ \log 2x & \log 2y & \log 2z \\ \log 3x & \log 3y & \log 3z \end{vmatrix} = 0$$

(OR)

- (b) Show that the vectors $\hat{i} 2\hat{j} + 3\hat{k}$, $-2\hat{i} + 3\hat{j} 4\hat{k}$, $-\hat{j} + 2\hat{k}$ are coplanar.
- 45. (a) Describe the interval(s) on which the function $h(x) = \begin{cases} x \sin \frac{1}{x}, & x \neq 0 \\ 0, & x = 0 \end{cases}$ is continuous.

(b) If
$$\sin y = x \sin(a+y)$$
, then prove that $\frac{dy}{dx} = \frac{\sin^2(a+y)}{\sin a}$, $a \neq n\pi$.

- 46. (a) Using the substitution $2x+1 = t^2$, show that $\int \frac{6x}{\sqrt{2x+1}} dx = 2(x-1)\sqrt{2x+1} + c.$ (OR)
 - (b) A construction company employs 2 executive engineers. Engineer-1 does the work for 60% of jobs of the company. Engineer-2 does the work for 40% of jobs of the company. It is known from the past experience that the probability of an error when engineer-1 does the work is 0.03, whereas the probability of an error in the work of engineer-2 is 0.04. Suppose a serious error occurs in the work, which engineer would you guess did the work?
- 47. (a) At a particular moment, a student needs to stop his speedybike to avoid a collision with the barrier ahead at a distance 40 metres away from him. Immediately he slows (retardation) the bike under braking at a rate of 8 metre/second². If the bike is moving at a speed of 24m/s, when the brakes are applied, would it stop before collision?

(OR)

(b) Find the separate equations of the pair of straight lines $2x^2 - xy - 3y^2 - 6x + 19y - 20 = 0$.
